

On the Foundations of Aromatic Reactivity

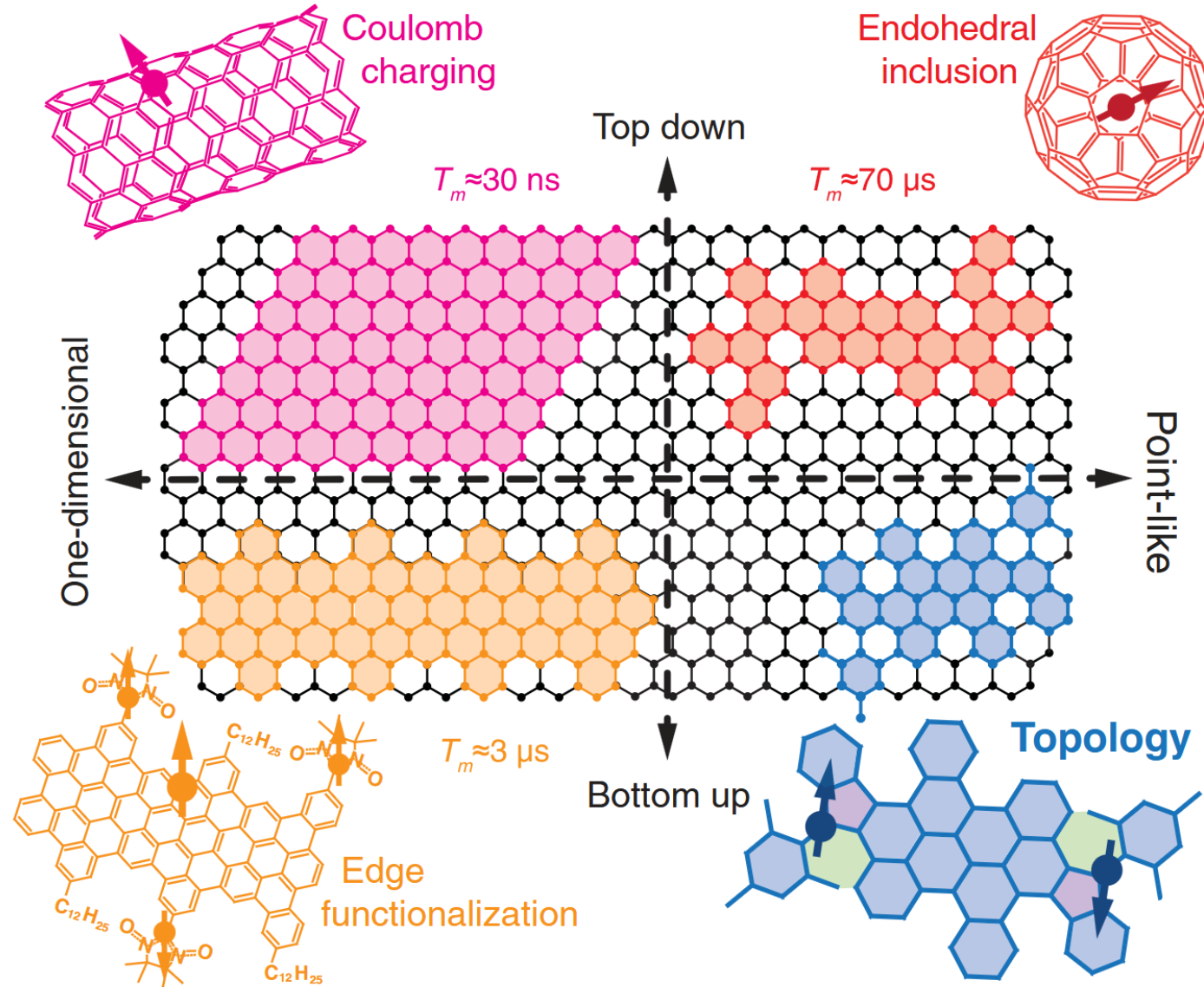
Lapo Bogani

University of Florence – Departments of Chemistry and Physics

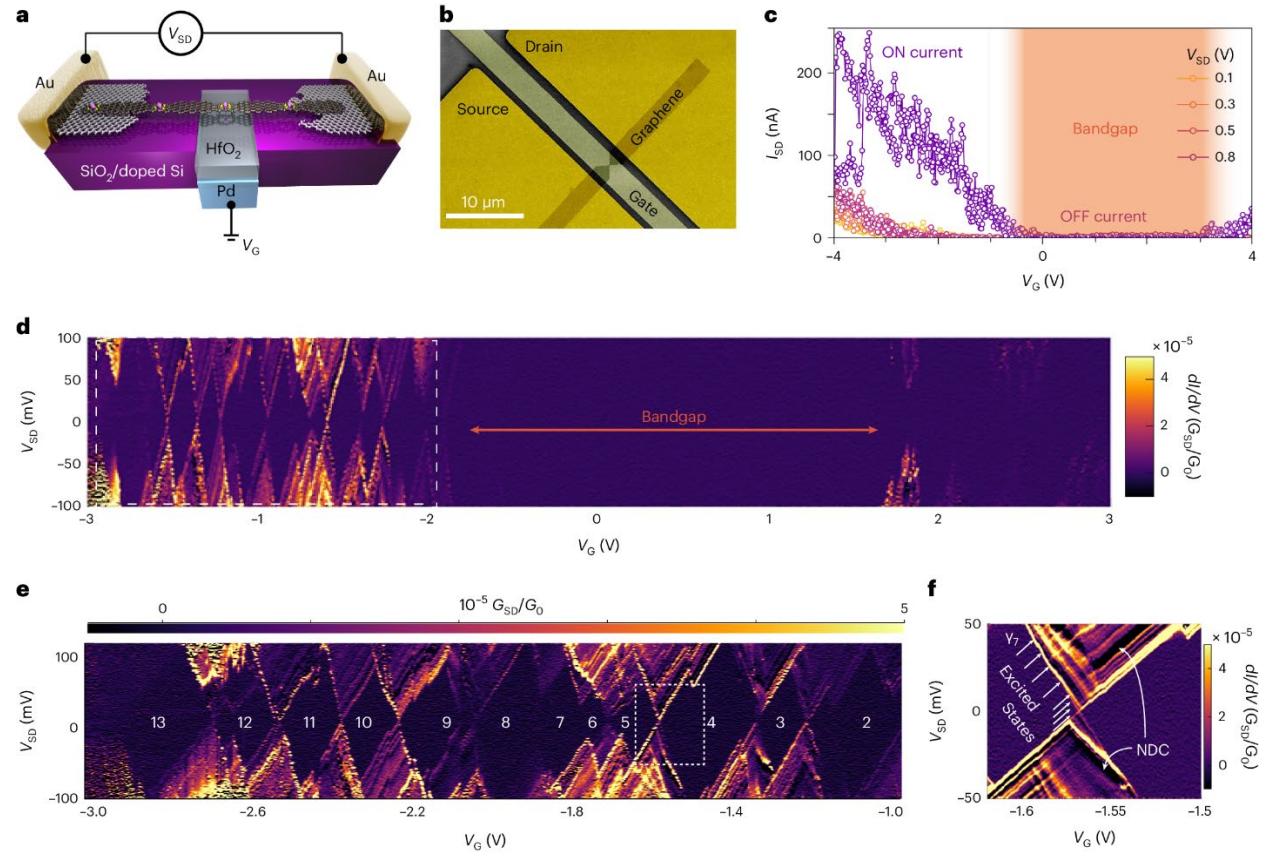
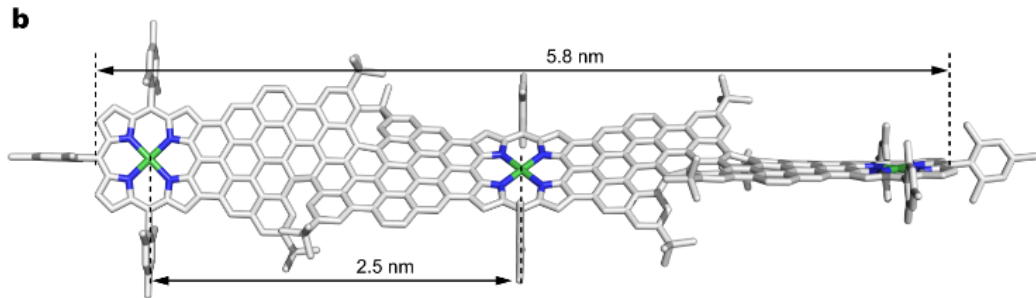
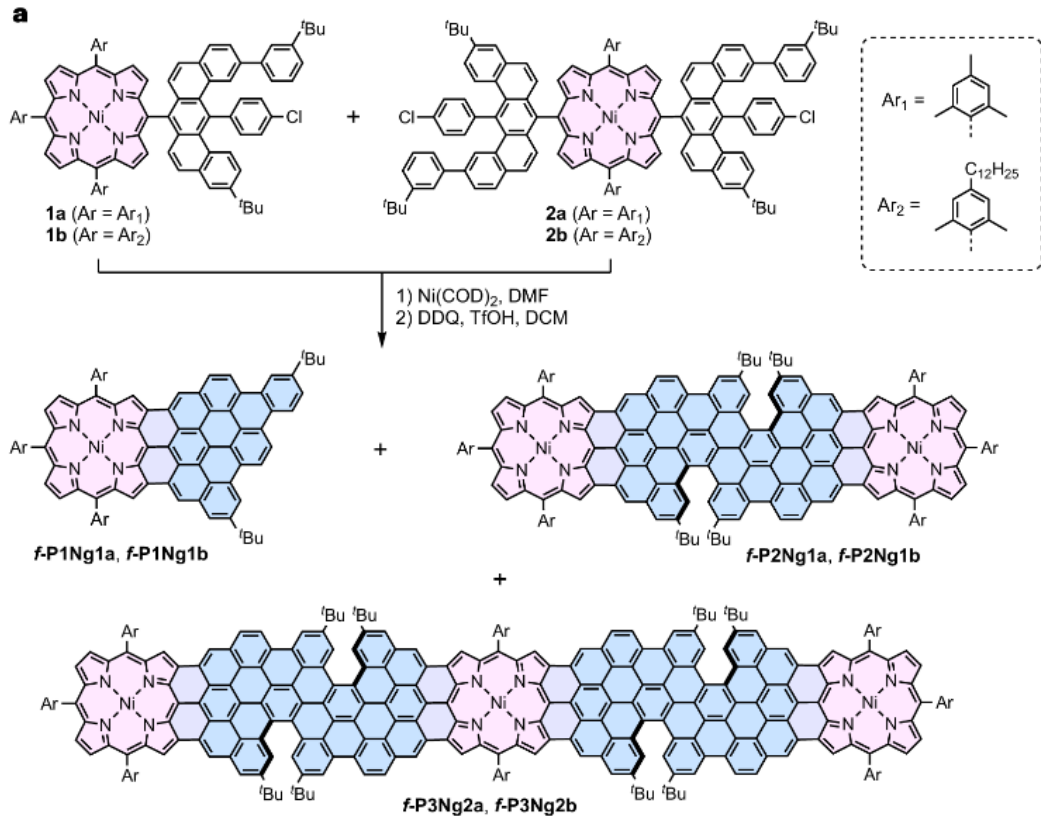
University of Oxford – Department of Materials



Molecular Graphenoids



Molecular Graphenoids

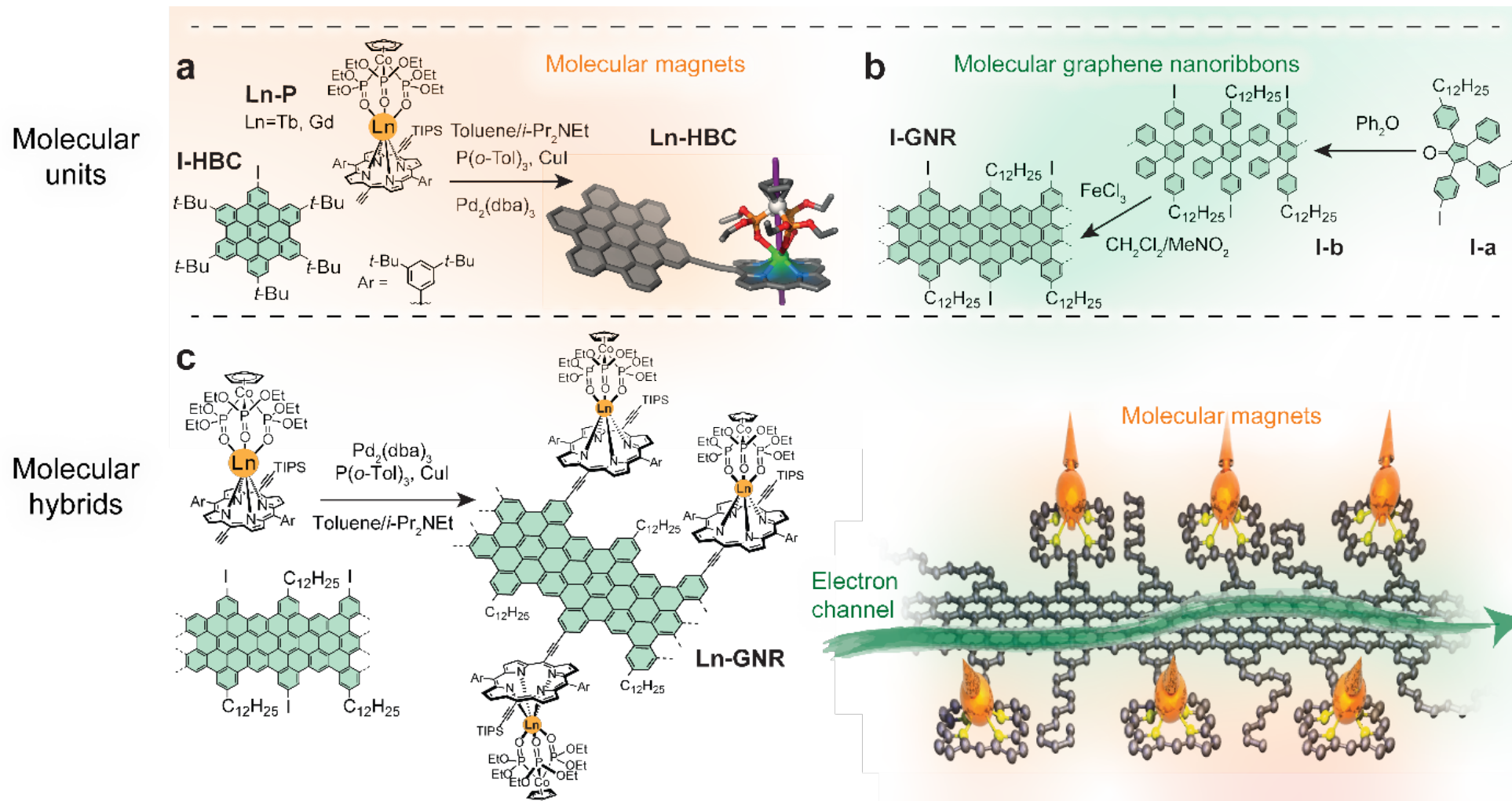


Nature Chemistry 2024

Porphyrin-fused graphene nanoribbons

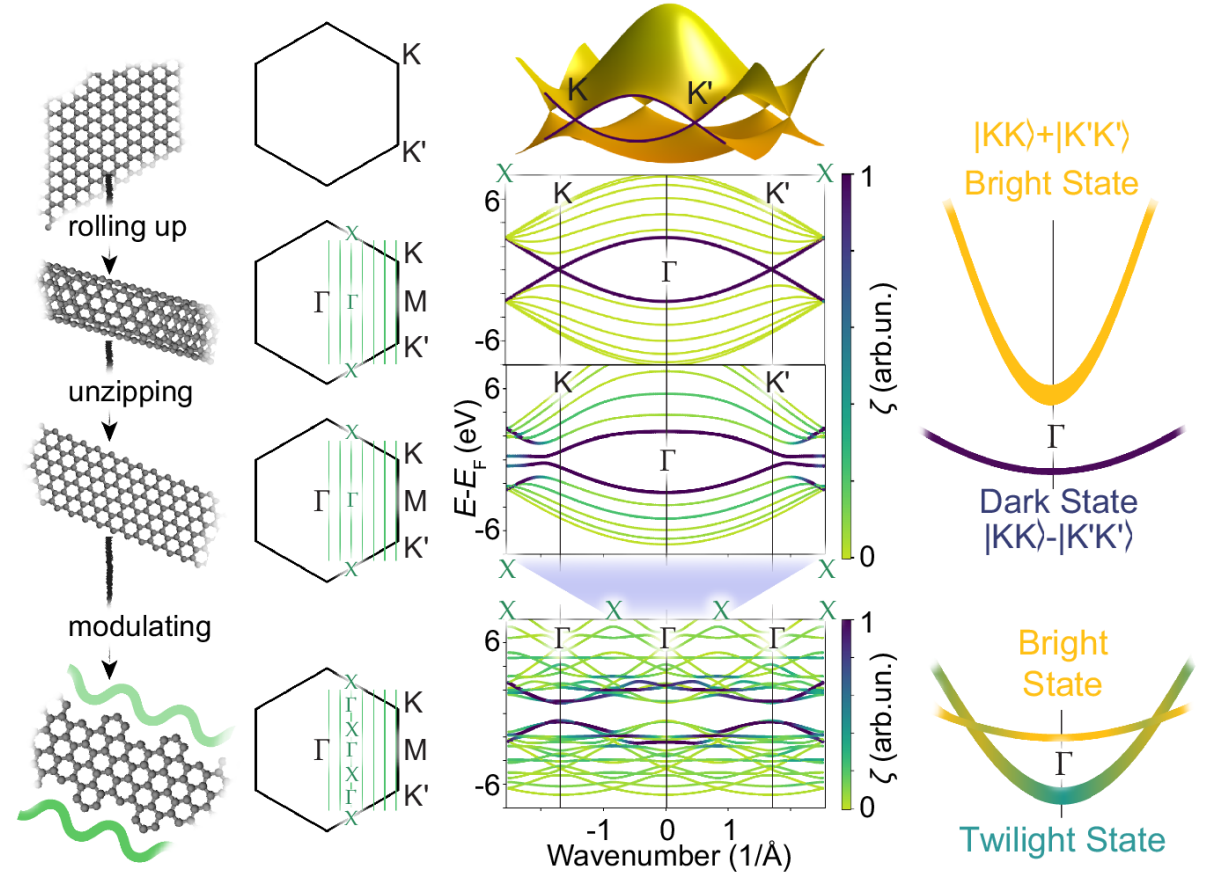
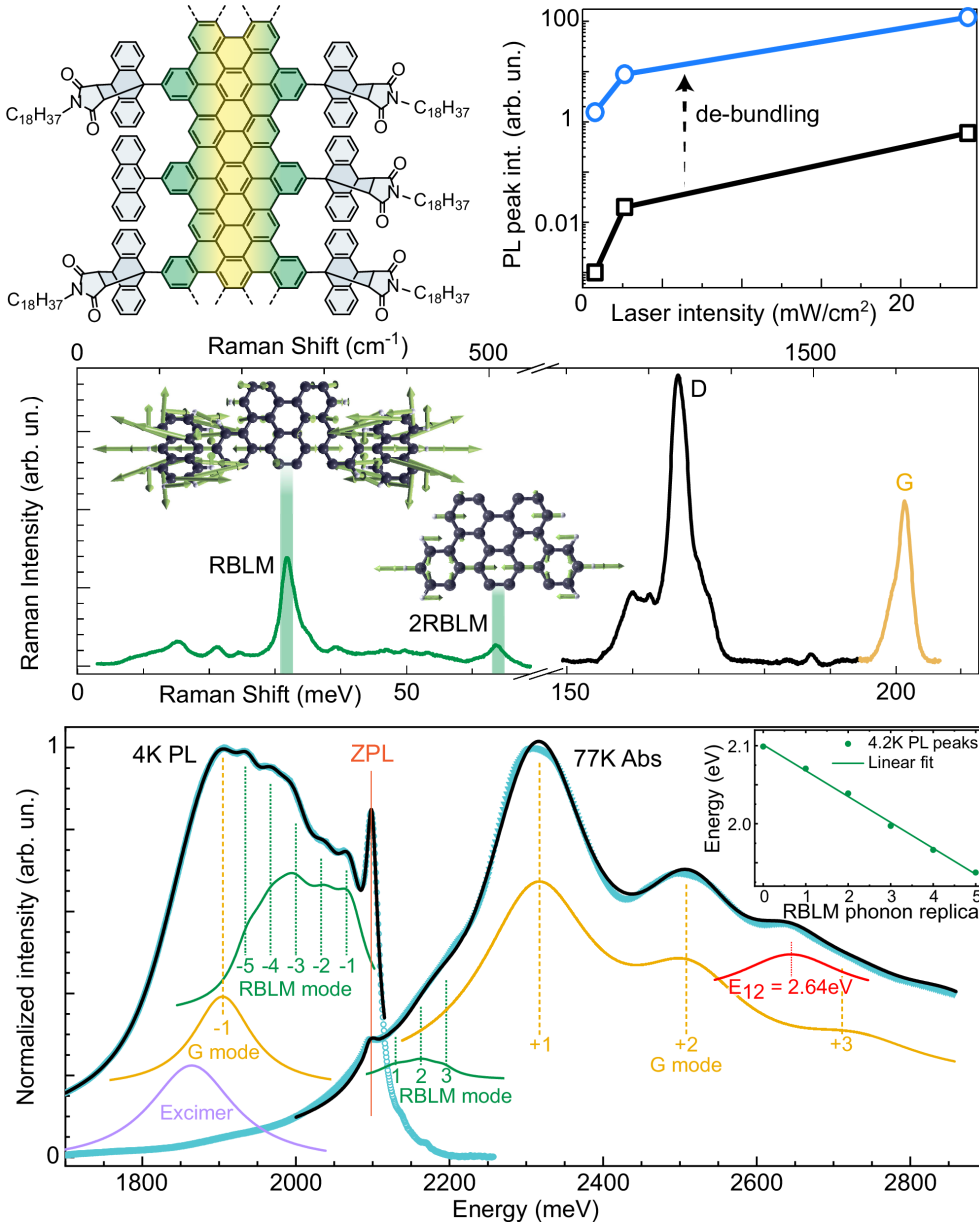
Qiang Chen , Alessandro Lodi, Heng Zhang, Alex Gee, Hai I. Wang, Fanmiao Kong, Michael Clarke, Matthew Edmondson, Jack Hart, James N. O'Shea, Wojciech Stawski, Jonathan Baugh, Akimitsu Narita, Alex Saywell, Mischa Bonn, Klaus Müllen, Lapo Bogani & Harry L. Anderson

Molecular Graphenoids



In preparation

Optics



Nature Communications 2024

Emissive brightening in molecular graphene nanoribbons by twilight states

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 Xinliang Feng^{3,4}, Moritz K. Riede¹, Lapo Bogani^{2,5} & Robin J. Nicholas¹

Something more fundamental?



[CONTRIBUTION FROM THE CHEMICAL LABORATORY OF THE UNIVERSITY OF CALIFORNIA.]

THE ATOM AND THE MOLECULE.

BY GILBERT N. LEWIS.

Received January 26, 1916.

In a paper entitled "Valence and Tautomerism"¹ I took occasion

¹ THIS JOURNAL, 35, 1448 (1913); see also the important article of Bray and Branch, *Ibid.*, 35, 1440 (1913).

G. N. Lewis 1916

W. Pauli 1926

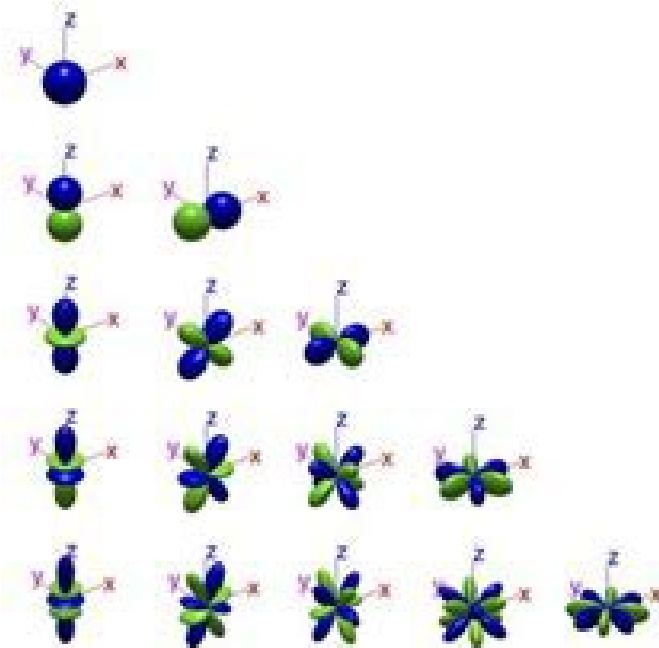
336

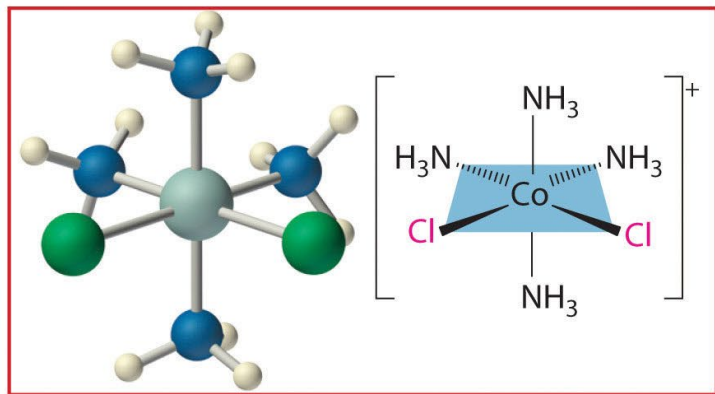
Über das Wasserstoffspektrum vom Standpunkt der neuen Quantenmechanik.

Von W. Pauli jr. in Hamburg.

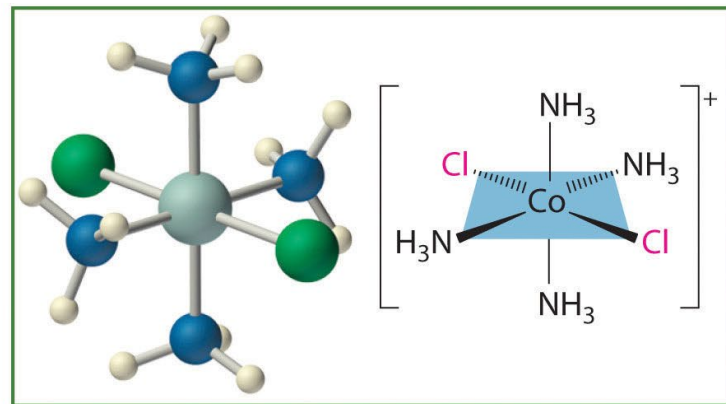
(Eingegangen am 17. Januar 1926.)

Es wird gezeigt, daß sich die Balmerterme eines Atoms mit einem einzigen Elektron aus der neuen Quantenmechanik richtig ergeben und daß die in der bisherigen Theorie aus den Zusatzverboten von singulären Bewegungen entstehenden Schwierigkeiten, die insbesondere im Falle der gekreuzten Felder zutage treten, in der neuen Theorie verschwinden. Auch die Beeinflussung des Wasserstoffspektrums durch äußere elektrische und magnetische Kraftfelder wird vom Standpunkt der neuen Quantenmechanik aus diskutiert. Die Berücksichtigung der Relativitätskorrekturen sowie die Berechnung der Übergangswahrscheinlichkeiten (Intensitäten) bleibt jedoch zunächst noch außer Betracht.





(a) Red form



(b) Green form



A. Werner **1913**

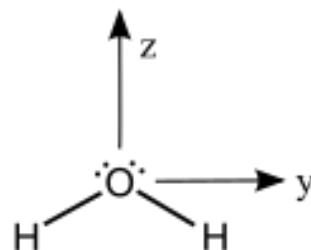
W. Cotton **1963**

CHEMICAL APPLICATIONS OF GROUP THEORY

F. Albert Cotton

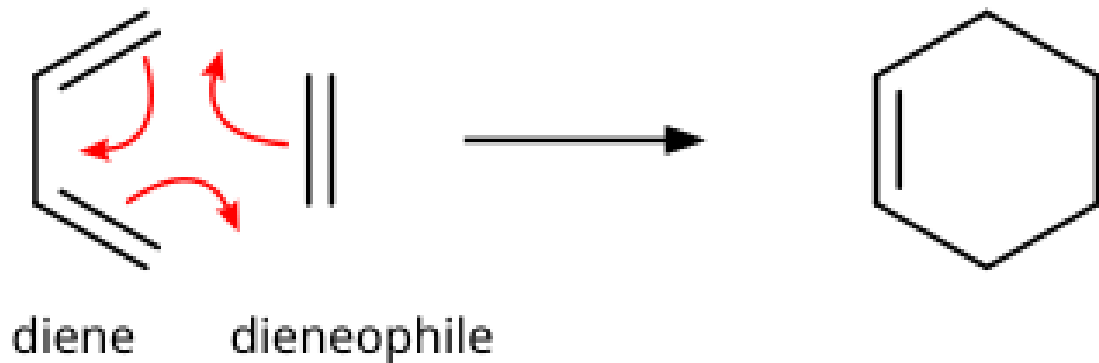
Department of Chemistry, Texas A&M University
College Station, Texas

THIRD EDITION



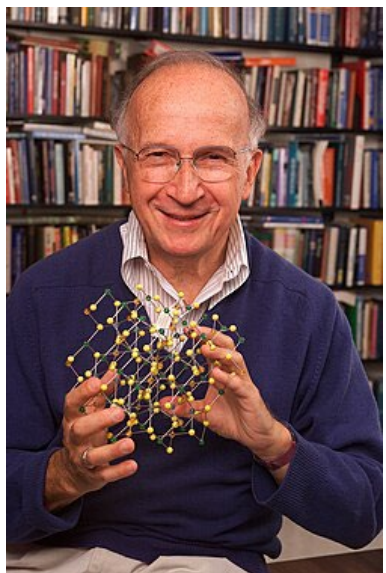
C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma'_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ_σ	2	0	0	2		

$$\Gamma_\sigma = A_1 + B_2$$



O. Diels, K. Alder **1950**

A. Hoffmann, K. Fukui **1983**



Symmetry operation
under two mirror planes

$\sigma_1\sigma_2$

Orbitals containing
the electrons

Symmetry of the
electrons under σ_1

Symmetry of the
electrons under σ_2

State symmetry

(AA)	$\pi_1^* - \pi_2^*$ —	$\pi_1^* - \pi_2^*$ —	$\pi_1^* - \pi_2^*$ —	$\pi_1^* - \pi_2^*$ —
(SA)	$\pi_1^* + \pi_2^*$ —	$(\pi_1^* + \pi_2^*)^1$ \updownarrow	$(\pi_1^* + \pi_2^*)^1$ \updownarrow	$(\pi_1^* + \pi_2^*)^2$ \updownarrow
(AS)	$(\pi_1 - \pi_2)^2$ \updownarrow	$(\pi_1 - \pi_2)^1$ \updownarrow	$(\pi_1 - \pi_2)^2$ \updownarrow	$\pi_1 - \pi_2$ —
(SS)	$(\pi_1 + \pi_2)^2$ \updownarrow	$(\pi_1 + \pi_2)^2$ \updownarrow	$(\pi_1 + \pi_2)^1$ \updownarrow	$(\pi_1 + \pi_2)^2$ \updownarrow
	S x S x A x A = S	S x S x A x S = A	S x A x A x S = S	S x S x S x S = S
	S x S x S x S = S	S x S x S x A = A	S x S x S x A = A	S x S x A x A = S
	SS	AA	AS	SS

Empiric Lab Rules

Underlying Reason

Draw molecular structures **1910s**

1930s Quantum numbers: n, l, m_l

d-orbital reactivity **1900s**

1960s Point group symmetry: $O_h, E...$

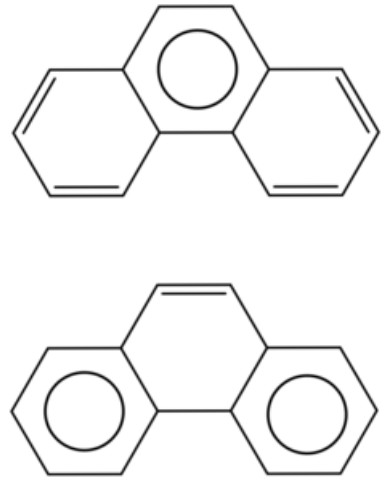
pericyclic stereochemistry **1930s**

1970s Symmetry-related selection

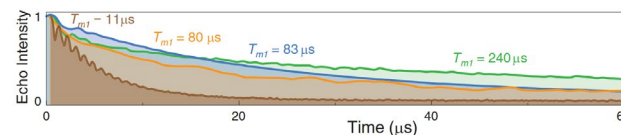
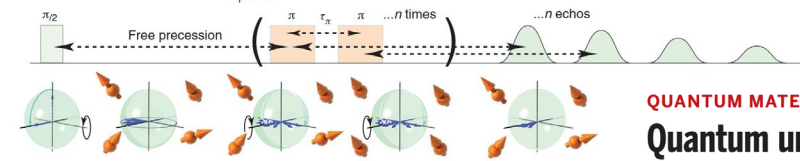
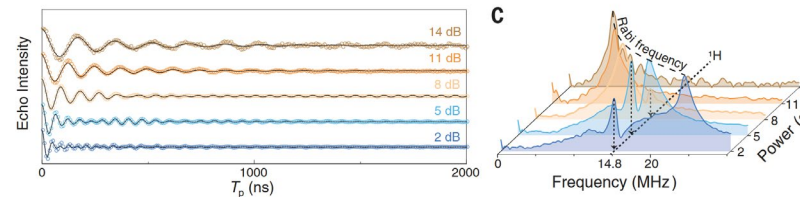
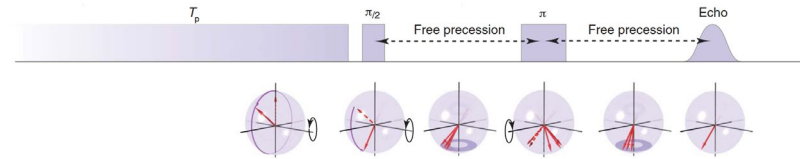
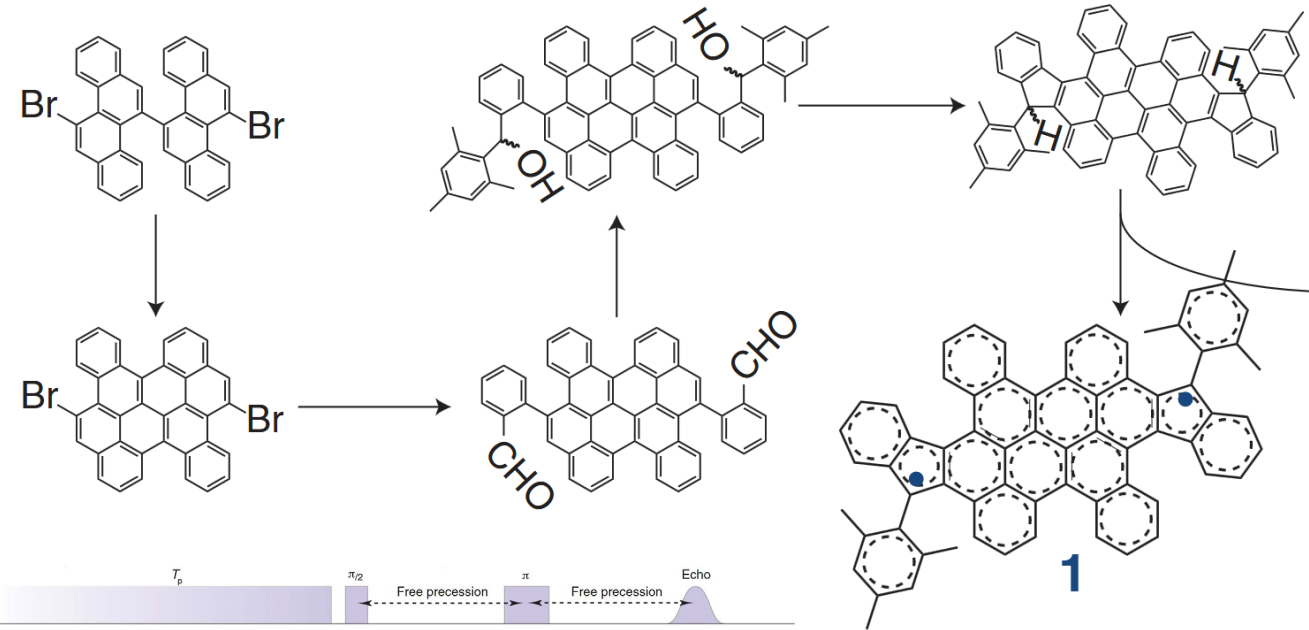
...more aplenty?

Polycyclic organic compounds

Clar's Sextet Rule **1970s**



The most stable structure is the one with more π sextets (circles).



Science **2019**

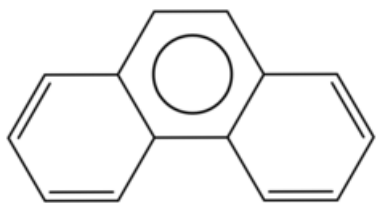
QUANTUM MATERIALS

Quantum units from the topological engineering of molecular graphenoids

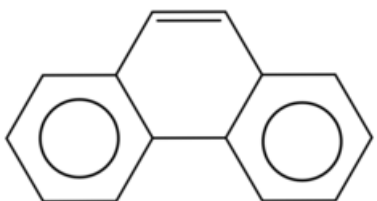
Federico Lombardi¹, Alessandro Lodi¹, Ji Ma², Junzhi Liu^{2*}, Michael Slota¹, Akimitsu Narita^{3†}, William K. Myers⁴, Klaus Müllen^{3‡}, Xinliang Feng², Lapo Bogani^{1§}

Polycyclic organic compounds

Clar's Sextet Rule **1970s**

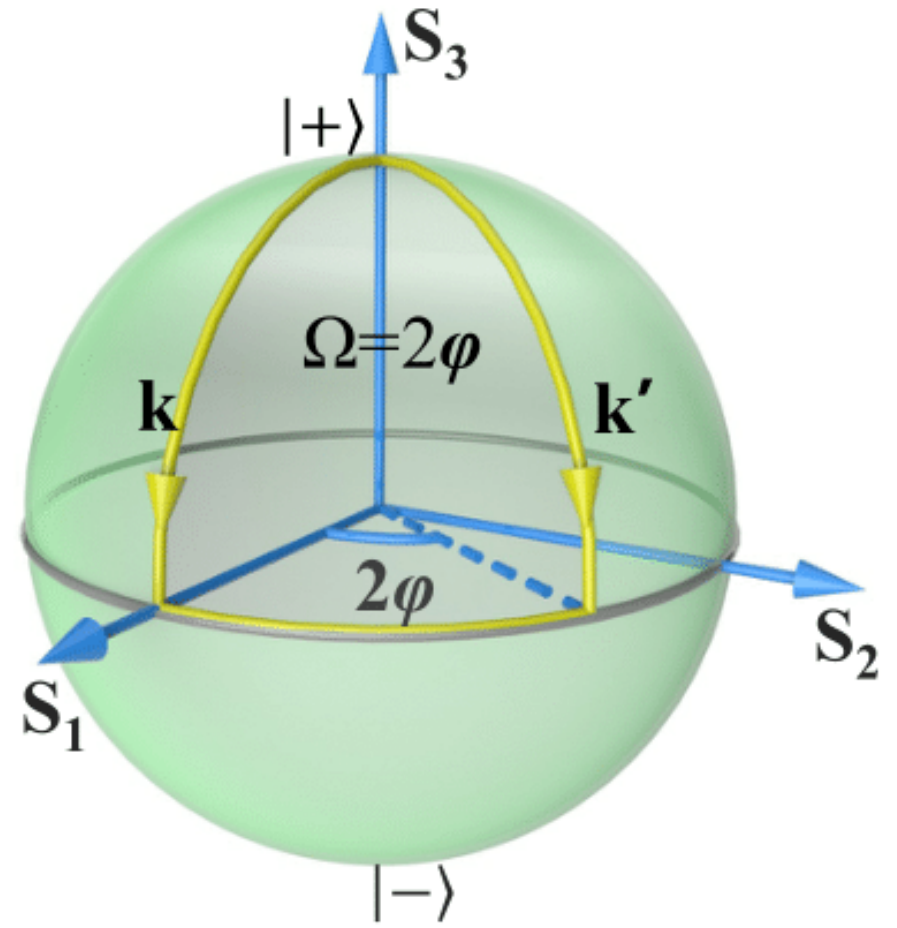
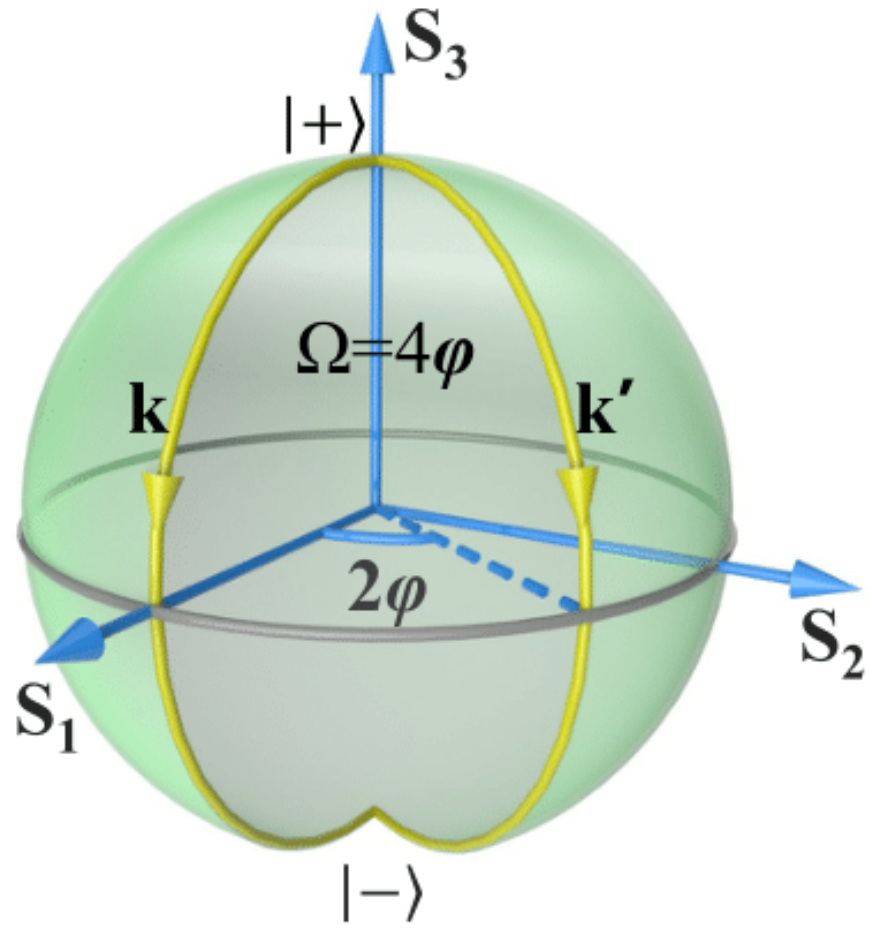


The most stable structure is the one with more π sextets (circles).

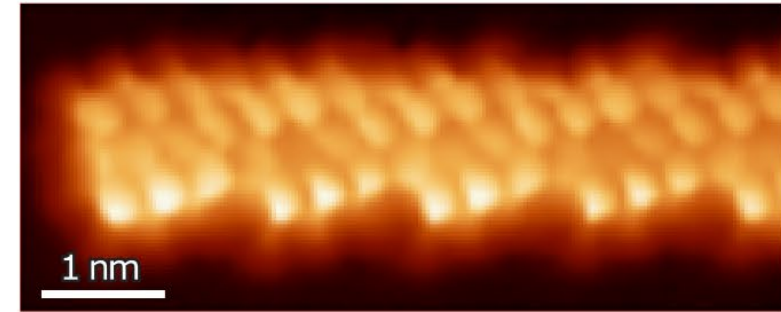
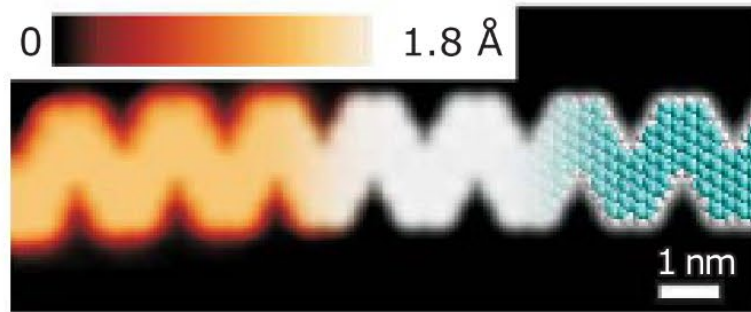
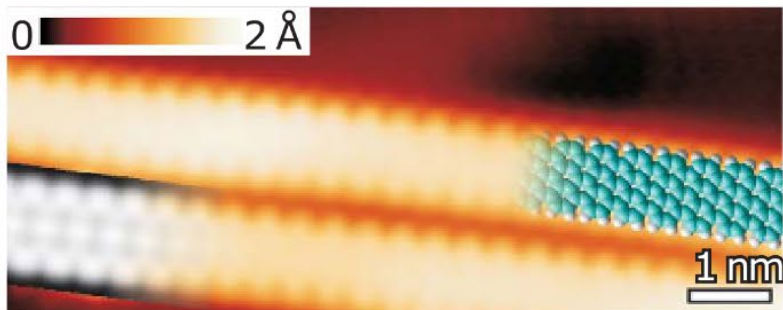
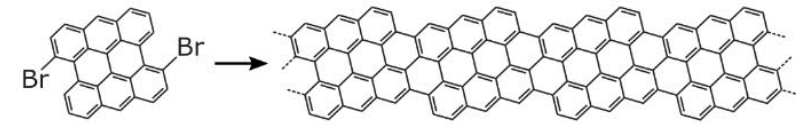
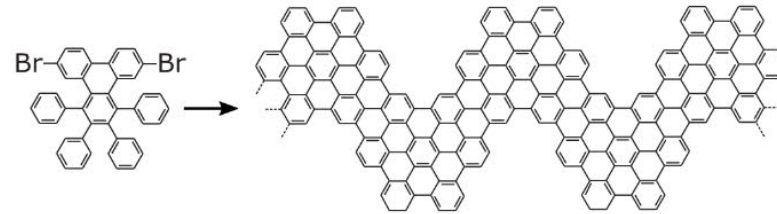
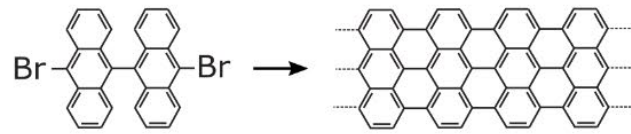
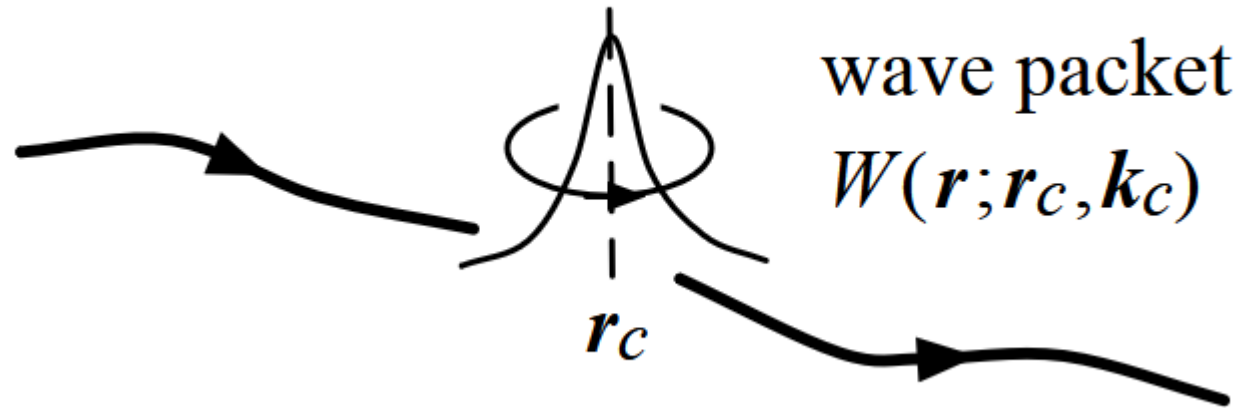


Quantum mechanical reason?

The Berry (Zak) Phase

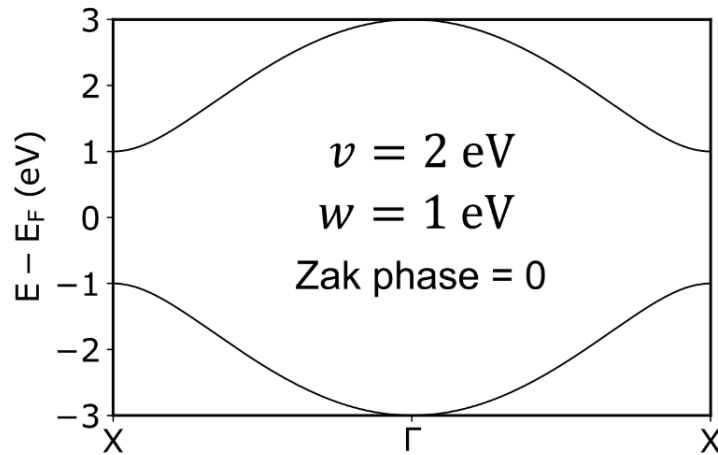


Electrons in Carbon

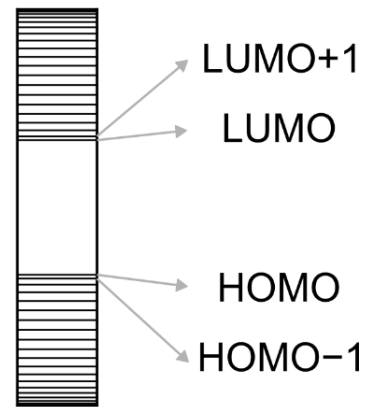


States created by the Zak phase

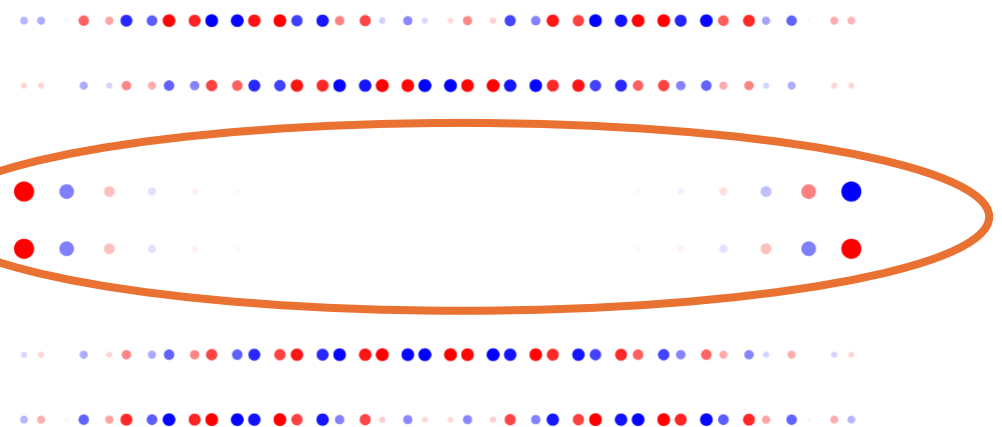
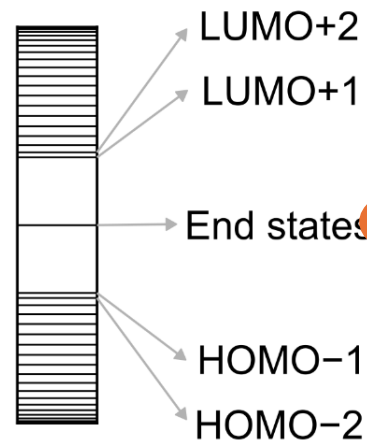
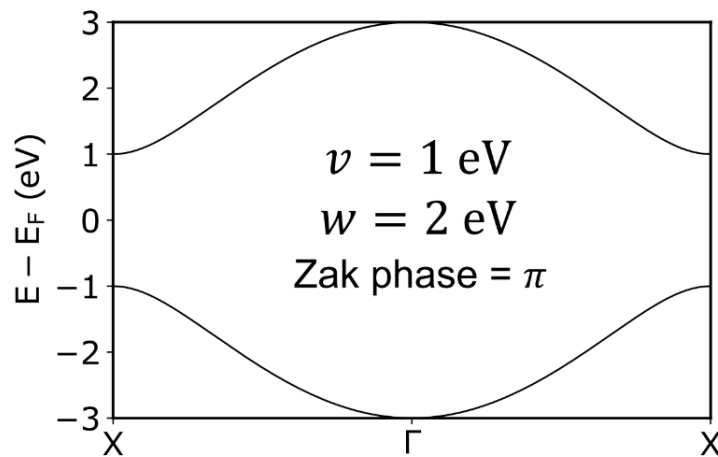
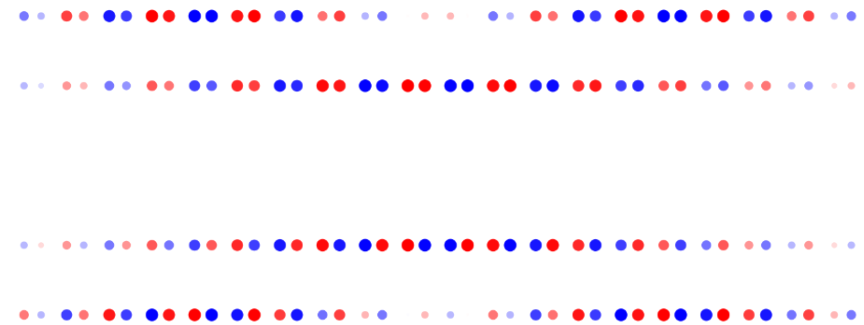
Band structure



Energy levels of finite chain



Wavefunctions of finite chain



A new number

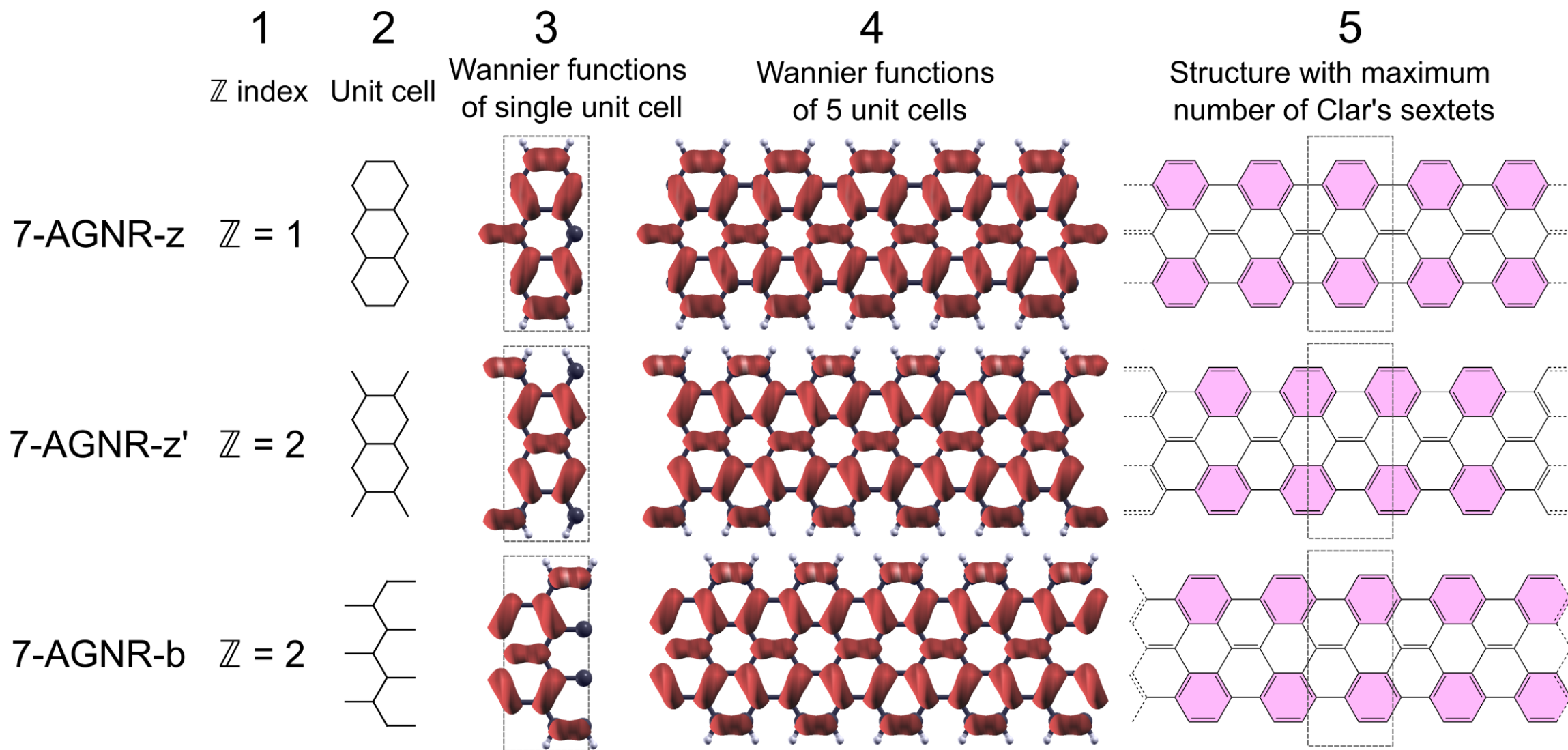
$$\gamma_n = \int_{\text{BZ}} A_n(k) dk \pmod{2\pi}, \quad A_n(k) = i \langle u_n(k) | \nabla_k | u_n(k) \rangle,$$

for all
electronic
states

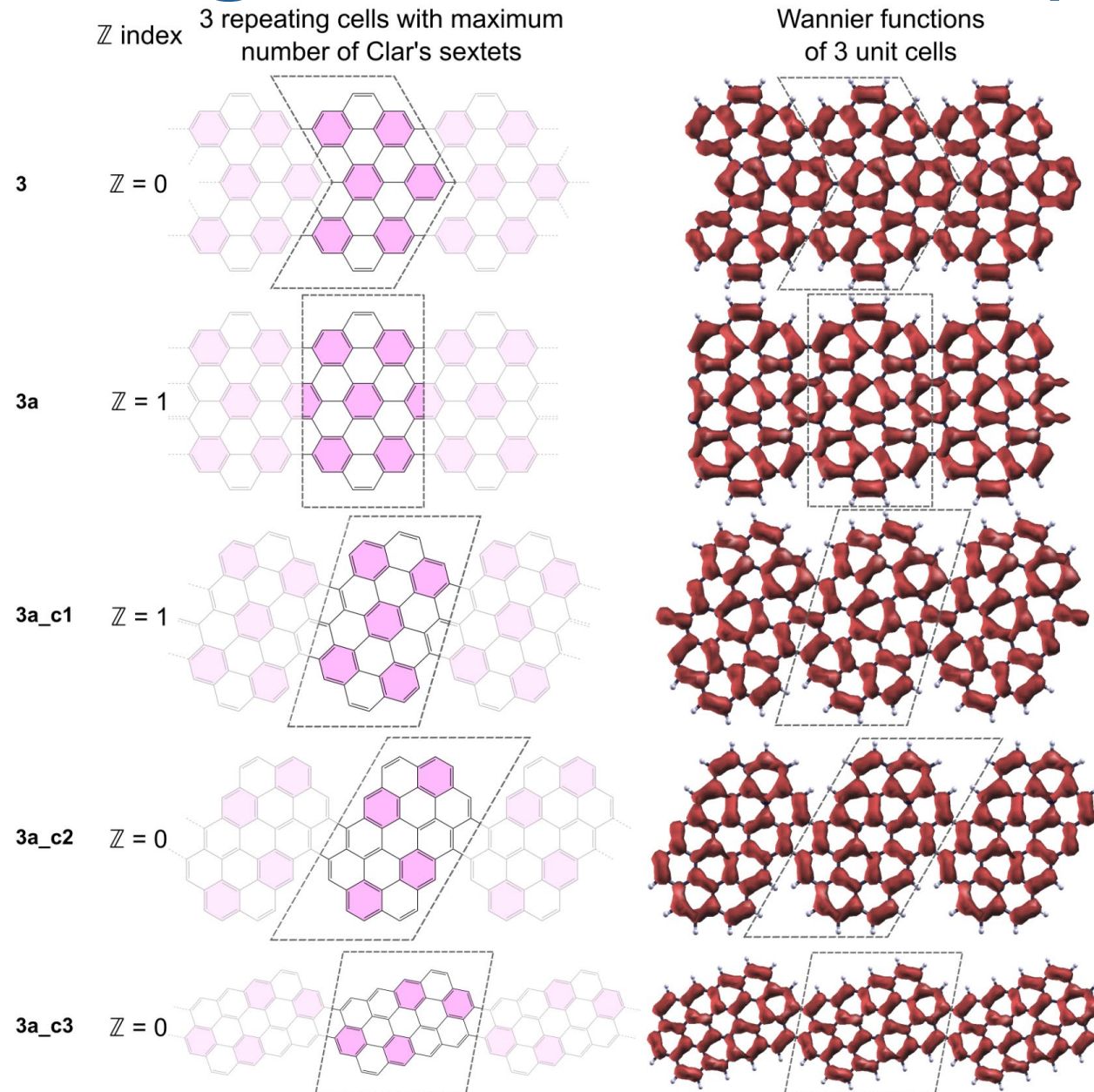
0 = trivial 1 = weird

Termination type	Zigzag ($N = \text{Odd}$)	Zigzag' ($N = \text{Odd}$)	Zigzag ($N = \text{Even}$)	Bearded ($N = \text{Even}$)
Unit cell shape				
Bulk Symmetry	Inversion/mirror	Inversion/mirror	Mirror	Inversion
Z_2	$\frac{1 + (-1)^{\lfloor \frac{N}{3} \rfloor + \lfloor \frac{N+1}{2} \rfloor}}{2}$	$\frac{1 - (-1)^{\lfloor \frac{N}{3} \rfloor + \lfloor \frac{N+1}{2} \rfloor}}{2}$	$\frac{1 - (-1)^{\lfloor \frac{N}{3} \rfloor}}{2}$	$\frac{1 - (-1)^{\lfloor \frac{N}{3} \rfloor}}{2}$

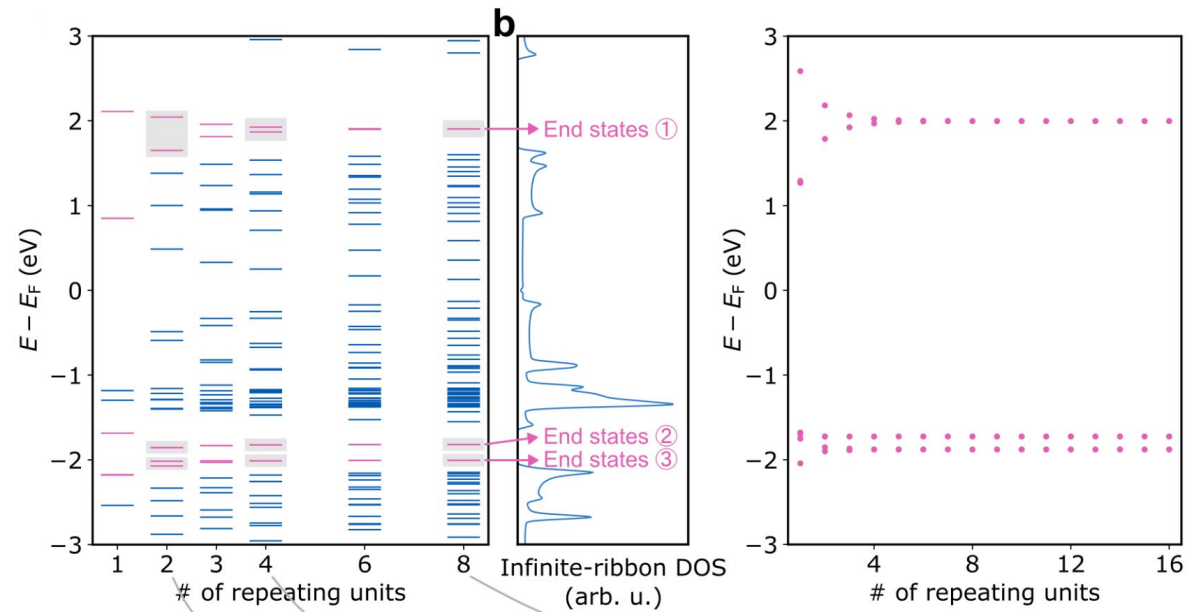
Is this connected to Clar's rule?



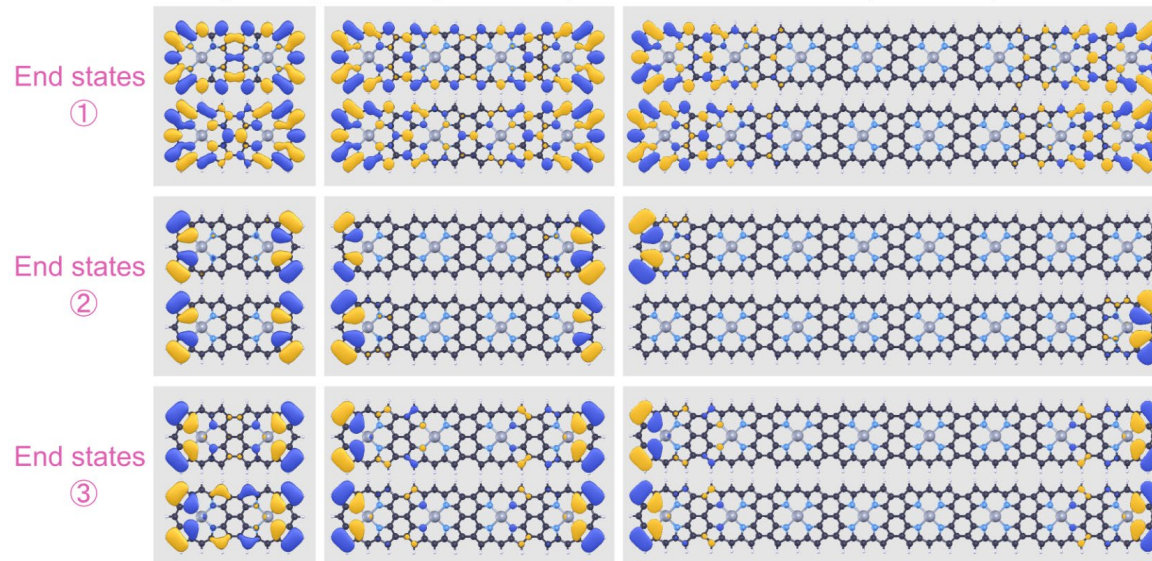
Exporting to different compounds



Extending Clar's rules



N=2 (dimer) N=4 (tetramer) N=8 (octamer)



Different molecules

Different sizes

Something more fundamental?

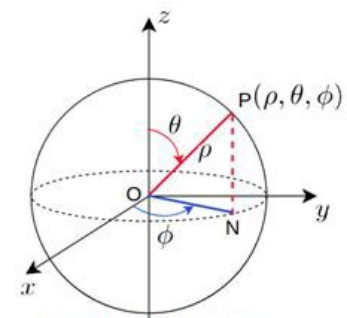
...maybe yes

Draw molecular structures **1910s**

d-orbital reactivity **1900s**

pericyclic stereochemistry **1930s**

1930s Quantum numbers: n, l, m_l



1960s Point group symmetry: $O_h, E...$

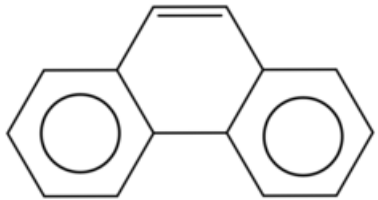
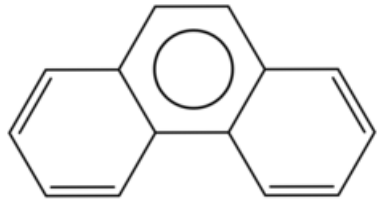
O_h	E	$8C_3$	$6C_2$	$6C_4$	$3C_2$	i	$6S_4$	$8S_6$	$3\sigma_h$	$6\sigma_d$		
A_{1g}	1	1	1	1	1	1	1	1	1	1		
A_{2g}	1	1	1	-1	-1	1	1	1	-1	-1		
E_g	2	-1	0	0	2	2	0	-1	2	0		$z^2, x^2 - y^2$
T_{1g}	3	0	-1	1	-1	3	1	0	-1	-1		
T_{2g}	3	0	1	-1	-1	3	-1	0	-1	1		(xy, xz, yz)
A_{1u}	1	1	1	1	1	-1	-1	-1	-1	-1		
A_{2u}	1	1	1	-1	-1	1	1	1	-1	1		
E_u	2	-1	0	0	2	-2	0	1	-2	0		
T_{1u}	3	0	-1	1	-1	-3	-1	0	1	1		(x, y, z)
T_{2u}	3	0	1	-1	-1	-3	1	0	1	-1		

1970s Symmetry-related selection

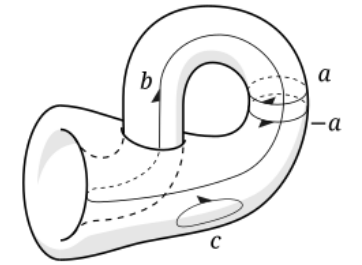
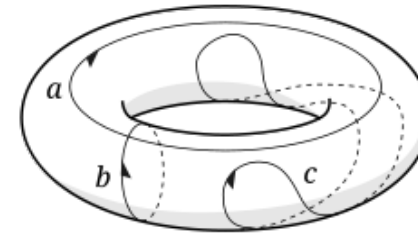
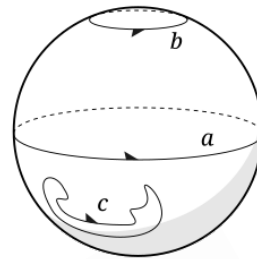
	σ	C_2
σ^*	 antisymmetric	 antisymmetric
π^*	 antisymmetric	 symmetric
π	 symmetric	 antisymmetric
σ	 symmetric	 symmetric

Polycyclic organic compounds

Clar's Sextet Rule **1970s**



The topology resulting from the reflections of the electronic waves



Thanks



F. Kong, A. Lombardi, S. Sopp, Z. Chen, X. Yao, C. Shen,
H. Chen, A. Lombardi, M. Reavley, R. Torres, M. Slota.

L. Briccolani, L. Chirolli, P. Fu.

H. L. Anderson, X. Feng, A. Narita, J. Wu, Z. Zhang.



StG-OptoQMol
CoG-MMGNRs

THE
ROYAL
SOCIETY



FONDAZIONE
CR FIRENZE



Is this connected to Clar's rule?

